

Derivation 1: N_2^*

$$\frac{dH^*}{dt} = 0 = \frac{cH(N_1a_1 + N_2a_2)}{1 + b(N_1a_1 + N_2a_2)} - mH$$

$$mH = \frac{cH(N_1a_1 + N_2a_2)}{1 + b(N_1a_1 + N_2a_2)}$$

$$m = \frac{c(N_1a_1 + N_2a_2)}{1 + b(N_1a_1 + N_2a_2)}$$

$$m(1 + b(N_1a_1 + N_2a_2)) = c(N_1a_1 + N_2a_2)$$

$$m + mb(N_1a_1 + N_2a_2) = c(N_1a_1 + N_2a_2)$$

$$m + mbN_1a_1 + mbN_2a_2 = cN_1a_1 + cN_2a_2$$

$$mbN_2a_2 - cN_2a_2 = cN_1a_1 - m - mbN_1a_1$$

$$N_2(mba_2 - ca_2) = cN_1a_1 - m - mbN_1a_1$$

$$N_2 = \frac{cN_1a_1 - m - mbN_1a_1}{(mba_2 - ca_2)}$$

$$N_2 = \frac{cN_1a_1 - m - mbN_1a_1}{a_2(mb - c)}$$

$$N_2 = \frac{cN_1a_1 - mbN_1a_1}{a_2(mb - c)} - \frac{m}{a_2(mb - c)}$$

$$N_2 = \frac{-N_1a_1(mb - c)}{a_2(mb - c)} - \frac{m}{a_2(mb - c)}$$

$$N_2^* = -\frac{a_1}{a_2}N_1 - \frac{m}{a_2(mb - c)}$$

Parameterize

$$D = \frac{m}{a_2(mb - c)}$$

$$A = -\frac{a_1}{a_2}$$

$$N_2^* = AN_1 - D$$

Derivation 2: H^*

$$\frac{dN_1^*}{dt} = 0 = R_1 \left(1 - \frac{N_1 + N_2\beta_{1,2}}{k_1} \right) - \left(\frac{N_1 H a_1}{1 + b(N_1 a_1 + N_2 a_2)} \right)$$

$$\left(\frac{N_1 H a_1}{1 + b(N_1 a_1 + N_2 a_2)} \right) = R_1 \left(1 - \frac{N_1 + N_2\beta_{1,2}}{k_1} \right)$$

$$H^* = R_1 \left(1 - \frac{N_1 + N_2\beta_{1,2}}{k_1} \right) \left(\frac{1 + b(N_1 a_1 + N_2 a_2)}{N_1 a_1} \right)$$

$$H^* = \frac{R_1 \left(1 - \frac{N_1 + N_2\beta_{1,2}}{k_1} \right) (1 + b(N_1 a_1 + N_2 a_2))}{N_1 a_1}$$

Substitute equilibrial value for N_2 in terms of N_1

$$H^* = \frac{R_1 \left(1 - \frac{N_1 + \left(-\frac{a_1}{a_2} N_1 - \frac{m}{a_2(mb - e)} \right) \beta_{1,2}}{k_1} \right) \left(1 + b \left(N_1 a_1 + \left(-\frac{a_1}{a_2} N_1 - \frac{m}{a_2(mb - e)} \right) a_2 \right) \right)}{N_1 a_1}$$

Substitute in composite parameters A and D

$$H^* = \frac{R_1 \left(1 - \frac{N_1^* + (AN_1^* - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1^* a_1 + (AN_1^* - D)a_2))}{N_1^* a_1}$$

Derivation 3: N_1^*

$$0 = \frac{dN_2^*}{dt} = R_2 \left(1 - \frac{N_2 + N_1\beta_{1,2}}{k_2} \right) - \left(\frac{N_2 H a_2}{1 + b(N_1 a_1 + N_2 a_2)} \right)$$

Substitute equilibrial values for N_2 and H in terms of N_1

$$0 = \frac{dN_2}{dt} = R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) - \left(\frac{(AN_1 - D) \left(\frac{R_1 \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1 a_1 + (AN_1 - D)a_2))}{N_1 a_1} \right) a_2}{1 + b(N_1 a_1 + (AN_1 - D)a_2)} \right)$$

Rearrange

$$\begin{aligned} R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) \\ = a_2 (AN_1 - D) R_1 \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1 a_1 + (AN_1 - D)a_2)) \left(\frac{1}{N_1 a_1} \right) \left(\frac{1}{1 + b(N_1 a_1 + (AN_1 - D)a_2)} \right) \end{aligned}$$

More rearranging

$$\begin{aligned} R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) \\ = a_2 \left(\frac{1}{N_1 a_1} \right) R_1 (AN_1 - D) \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1 a_1 + (AN_1 - D)a_2)) \left(\frac{1}{1 + b(N_1 a_1 + (AN_1 - D)a_2)} \right) \end{aligned}$$

More rearranging

$$R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) = a_2 \frac{1}{a_1} \frac{1}{N_1} R_1(AN_1 - D) \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1a_1 + (AN_1 - D)a_2)) \left(\frac{1}{1 + b(N_1a_1 + (AN_1 - D)a_2)} \right)$$

Substitute

$$a_2 \frac{1}{a_1} = \frac{a_2}{a_1} = -\frac{1}{A}$$

$$R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) = -\frac{1}{AN_1} R_1(AN_1 - D) \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right) (1 + b(N_1a_1 + (AN_1 - D)a_2)) \left(\frac{1}{1 + b(N_1a_1 + (AN_1 - D)a_2)} \right)$$

Cancel

$$R_2 \left(1 - \frac{(AN_1 - D) + N_1\beta_{2,1}}{k_2} \right) = -\frac{1}{AN_1} R_1(AN_1 - D) \left(1 - \frac{N_1 + (AN_1 - D)\beta_{1,2}}{k_1} \right)$$

Rearrange growth terms

$$R_2 \left(\frac{k_2 - (AN_1 - D) - N_1\beta_{2,1}}{k_2} \right) = -\frac{1}{AN_1} R_1(AN_1 - D) \left(\frac{k_1 - N_1 - (AN_1 - D)\beta_{1,2}}{k_1} \right)$$

Rearrange

$$\frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1\beta_{2,1}) = -\frac{1}{AN_1} (AN_1 - D) (k_1 - N_1 - (AN_1 - D)\beta_{1,2})$$

Start multiplying out the right side

$$\begin{aligned}\frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \left(\frac{D}{AN_1} - 1 \right) (k_1 - N_1 - (AN_1 - D) \beta_{1,2}) \\ \frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \frac{D}{AN_1} (k_1 - N_1 - (AN_1 - D) \beta_{1,2}) - (k_1 - N_1 - (AN_1 - D) \beta_{1,2}) \\ \frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \left(\frac{D k_1}{AN_1} - \frac{D}{A} - \frac{D}{AN_1} (AN_1 - D) \beta_{1,2} \right) - (k_1 - N_1 - (AN_1 - D) \beta_{1,2}) \\ \frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \frac{D k_1}{AN_1} - \frac{D}{A} - D \beta_{1,2} + \frac{D^2 \beta_{1,2}}{AN_1} - (k_1 - N_1 - (AN_1 - D) \beta_{1,2}) \\ \frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \frac{D k_1}{AN_1} - \frac{D}{A} - D \beta_{1,2} + \frac{D^2 \beta_{1,2}}{AN_1} - k_1 + N_1 + AN_1 \beta_{1,2} - D \beta_{1,2}\end{aligned}$$

Rearrange

$$\begin{aligned}\frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \frac{D k_1 + D^2 \beta_{1,2}}{AN_1} - \frac{D}{A} - k_1 + N_1 + AN_1 \beta_{1,2} - 2D \beta_{1,2} \\ \frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) &= \frac{D k_1 + D^2 \beta_{1,2}}{AN_1} + N_1 + AN_1 \beta_{1,2} - 2D \beta_{1,2} - \frac{D}{A} - k_1\end{aligned}$$

Isolate term with N_1 in denominator

$$\frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) - N_1 - AN_1 \beta_{1,2} + 2D \beta_{1,2} + \frac{D}{A} + k_1 = \frac{D k_1 + D^2 \beta_{1,2}}{AN_1}$$

Multiply both sides by AN_1

$$AN_1 \left(\frac{R_2 k_1}{R_1 k_2} (k_2 - (AN_1 - D) - N_1 \beta_{2,1}) - N_1 - AN_1 \beta_{1,2} + 2D \beta_{1,2} + \frac{D}{A} + k_1 \right) = D k_1 + D^2 \beta_{1,2}$$

$$\frac{AN_1R_2k_1}{R_1k_2}(k_2 - (AN_1 - D) - N_1\beta_{2,1}) - AN_1^2 - (AN_1)^2\beta_{1,2} + 2AN_1D\beta_{1,2} + \frac{AN_1D}{A} + AN_1k_1 = Dk_1 + D^2\beta_{1,2}$$

$$\frac{AN_1R_2k_1}{R_1} - \frac{AN_1R_2k_1}{R_1k_2}(AN_1 - D) - \frac{AN_1^2R_2k_1\beta_{2,1}}{R_1k_2} - AN_1^2 - (AN_1)^2\beta_{1,2} + 2AN_1D\beta_{1,2} + \frac{AN_1D}{A} + AN_1k_1 = Dk_1 + D^2\beta_{1,2}$$

$$\frac{AN_1R_2k_1}{R_1} - \frac{(AN_1)^2R_2k_1}{R_1k_2} + \frac{AN_1R_2k_1D}{R_1k_2} - \frac{AN_1^2R_2k_1\beta_{2,1}}{R_1k_2} - AN_1^2 - (AN_1)^2\beta_{1,2} + 2AN_1D\beta_{1,2} + \frac{AN_1D}{A} + AN_1k_1 = Dk_1 + D^2\beta_{1,2}$$

Rearrange

$$- \frac{(AN_1)^2R_2k_1}{R_1k_2} - \frac{AN_1^2R_2k_1\beta_{2,1}}{R_1k_2} - AN_1^2 - (AN_1)^2\beta_{1,2} + \frac{AN_1R_2k_1}{R_1} + \frac{AN_1R_2k_1D}{R_1k_2} + 2AN_1D\beta_{1,2} + \frac{AN_1D}{A} + AN_1k_1 = Dk_1 + D^2\beta_{1,2}$$

$$\left(- \frac{A^2R_2k_1}{R_1k_2} - \frac{AR_2k_1\beta_{2,1}}{R_1k_2} - A - A^2\beta_{1,2} \right) N_1^2 + \left(\frac{AR_2k_1}{R_1} + \frac{AR_2k_1D}{R_1k_2} + 2AD\beta_{1,2} + \frac{AD}{A} + Ak_1 \right) N_1 = Dk_1 + D^2\beta_{1,2}$$

$$\left(- \frac{A^2R_2k_1}{R_1k_2} - \frac{AR_2k_1\beta_{2,1}}{R_1k_2} - A - A^2\beta_{1,2} \right) N_1^2 + \left(\frac{AR_2k_1}{R_1} + \frac{AR_2k_1D}{R_1k_2} + 2AD\beta_{1,2} + \frac{AD}{A} + Ak_1 \right) N_1 - (Dk_1 + D^2\beta_{1,2}) = 0$$

$$\left(- \frac{A^2R_2k_1}{R_1k_2} - A^2\beta_{1,2} - \frac{AR_2k_1\beta_{2,1}}{R_1k_2} - A \right) N_1^2 + \left(\frac{AR_2k_1}{R_1} + \frac{AR_2k_1D}{R_1k_2} + 2AD\beta_{1,2} + D + Ak_1 \right) N_1 - (Dk_1 + D^2\beta_{1,2}) = 0$$

Substitute in composite parameters

$$P = \frac{R_2}{R_1}$$

$$\left(- \frac{A^2Pk_1}{k_2} - A^2\beta_{1,2} - \frac{APk_1\beta_{2,1}}{k_2} - A \right) N_1^2 + \left(APk_1 + \frac{APk_1D}{k_2} + 2AD\beta_{1,2} + D + Ak_1 \right) N_1 - (Dk_1 + D^2\beta_{1,2}) = 0$$

$$G = \frac{APk_1}{k_2}$$

$$(-GA - A^2\beta_{1,2} - G\beta_{2,1} - A)N_1^2 + (APk_1 + GD + 2AD\beta_{1,2} + D + Ak_1)N_1 - (Dk_1 + D^2\beta_{1,2}) = 0$$

Rearrange

$$(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})N_1^2 + (APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D)N_1 - (Dk_1 + D^2\beta_{1,2}) = 0$$

Quadratic formula

$$N_1^* = \frac{-y \pm \sqrt{y^2 - 4xz}}{2x}$$

$$x = -A^2\beta_{1,2} - A - GA - G\beta_{2,1}$$

$$y = APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D$$

$$z = -Dk_1 - D^2\beta_{1,2}$$

$$N_1^* = \frac{-(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) \pm \sqrt{(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D)^2 - 4(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})(-Dk_1 - D^2\beta_{1,2})}}{2(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})}$$

Expand

$$N_1^* = \frac{-APk_1 - 2AD\beta_{1,2} - Ak_1 - GD - D \pm \sqrt{\begin{aligned} &(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D)^2 + \\ &\left(\begin{aligned} &-4A^2\beta_{1,2}Dk_1 - 4ADk_1 - 4GADk_1 - 4G\beta_{2,1}Dk_1 - \\ &4A^2\beta_{1,2}D^2\beta_{1,2} - 4AD^2\beta_{1,2} - 4GAD^2\beta_{1,2} - 4G\beta_{1,2}D^2\beta_{1,2} \end{aligned} \right) \end{aligned}}}{2(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})}$$

Expand y^2 term

$$\begin{aligned}
y^2 &= (APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D)^2 \\
&= APk_1(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) + 2AD\beta_{1,2}(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) \\
&\quad + Ak_1(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) + GD(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) \\
&\quad + D(APk_1 + 2AD\beta_{1,2} + Ak_1 + GD + D) \\
y^2 &= (A^2P^2k_1^2 + 2A^2D\beta_{1,2}Pk_1 + A^2Pk_1^2 + APk_1GD + APk_1D) + (2A^2D\beta_{1,2}Pk_1 + 4A^2D^2\beta_{1,2}^2 + 2A^2D\beta_{1,2}k_1 + 2AD^2\beta_{1,2}G + 2AD^2\beta_{1,2}) \\
&\quad + (A^2Pk_1^2 + 2A^2k_1D\beta_{1,2} + A^2k_1^2 + Ak_1GD + Ak_1D) + (GDAPk_1 + GD2AD\beta_{1,2} + GDAk_1 + G^2D^2 + GD^2) \\
&\quad + (DAPk_1 + 2AD^2\beta_{1,2} + DAK_1 + GD^2 + D^2) \\
y^2 &= A^2P^2k_1^2 + 2A^2Pk_1^2 + A^2k_1^2 + 4A^2D^2\beta_{1,2}^2 + 4A^2D\beta_{1,2}Pk_1 + 4A^2D\beta_{1,2}k_1 + 4AD^2\beta_{1,2}G + 4AD^2\beta_{1,2} + 2APk_1GD + 2APk_1D \\
&\quad + 2Ak_1GD + 2Ak_1D + G^2D^2 + 2GD^2 + D^2
\end{aligned}$$

Combine everything under the radical ($y^2 - 4xz$)

$$\begin{aligned}
&y^2 - 4xz \\
&= \left(A^2P^2k_1^2 + 2A^2Pk_1^2 + A^2k_1^2 + 4A^2D^2\beta_{1,2}^2 + 4A^2D\beta_{1,2}Pk_1 + 4A^2D\beta_{1,2}k_1 + 4AD^2\beta_{1,2}G + 4AD^2\beta_{1,2} + 2APk_1GD + 2APk_1D + 2Ak_1GD \right. \\
&\quad \left. + 2Ak_1D + G^2D^2 + 2GD^2 + D^2 - 4A^2\beta_{1,2}Dk_1 - 4ADk_1 - 4GADk_1 - 4G\beta_{2,1}Dk_1 - 4A^2\beta_{1,2}D^2\beta_{1,2} - 4AD^2\beta_{1,2} - 4GAD^2\beta_{1,2} - 4G\beta_{2,1}D^2\beta_{1,2} \right) \\
y^2 - 4xz &= A^2P^2k_1^2 + 2A^2Pk_1^2 + A^2k_1^2 + 4A^2D\beta_{1,2}Pk_1 + 0A^2D\beta_{1,2}k_1 + 2APk_1GD + 2APk_1D - 2Ak_1D + G^2D^2 + 2GD^2 + D^2 - 2GADk_1 \\
&\quad - 4G\beta_{2,1}Dk_1 - 4G\beta_{2,1}D^2\beta_{1,2}
\end{aligned}$$

Combine quadratic terms back into equation

$$N_1^* = \frac{\left(\frac{(-APk_1 - 2AD\beta_{1,2} - Ak_1 - GD - D) - \sqrt{A^2P^2k_1^2 + 2A^2Pk_1^2 + A^2k_1^2 + 4A^2D\beta_{1,2}Pk_1 + 2APk_1GD + 2APk_1D - 2Ak_1D + G^2D^2 + 2GD^2 + D^2 - 2GADk_1 - 4G\beta_{2,1}Dk_1 - 4G\beta_{1,2}D^2\beta_{1,2}}}{2(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})} \right)}{2(-A^2\beta_{1,2} - A - GA - G\beta_{2,1})}$$

Appendix 3

Parameter estimates (highlighted) with supporting values listed beneath

Model param.	Description	Units	Est.* (min- max)	Est. units	Study	Location	Source	Model value used
N_1	Plant 1 (<i>Amorpha</i>) mass	Plant mass	294000- 441000	g/ha				—
					<i>Amorpha</i> densities in the presence of cattle grazing	Tallgrass prairie, Kansas	Hickman and Hartnett 2002	
			25300 11.6- 17.4	stems/ha g/stem	<i>Amorpha</i> min/max mass per stem	Tallgrass prairie, Kansas	Towne and Knapp 1996	
N_2	Plant 2 (<i>Dalea</i>) mass	Plant mass	229-582	g/ha				—
					<i>Dalea</i> densities in presence of voles	Tallgrass prairie, Kansas	Howe et al 2002	
			200 1.14- 2.91	stems/ha g/stem	<i>Dalea</i> min/max mass per stem	Tallgrass prairie, Kansas	Towne and Knapp 1996	
H	Herbivore mass	Herbivore mass	72-6200	g/ha				—
					<i>Microtus ochrogaster</i> and <i>pennsylvanicus</i> densities	Range-wide, North America	Taitt and Krebs 1981	
			2-172 35.972	ind/ha g/ind	<i>Microtus ochrogaster</i> and <i>pennsylvanicus</i> mean mass	Tallgrass prairie, Iowa	Pers. obs.	

Model param.	Description	Units	Est.* (min- max)	Est. units	Study	Location	Source	Model value used
R_1	Growth rate of plant 1	N_1 mass/time	3270- 60100	g/ha/day	Tallgrass prairie forb growth rates	Tallgrass prairie, Kansas	Briggs and Knapp 2001	4000
R_2	Growth rate of plant 2	N_2 mass/time	3270- 60100	g/ha/day	Tallgrass prairie forb growth rates	Tallgrass prairie, Kansas	Briggs and Knapp 2001	4000
k_1	Plant 1 carrying capacity	N_1 mass	172000- 288000	g/ha	<i>Amorpha</i> biomass in unburned fields	Tallgrass prairie, Kansas	Towne and Knapp 1996	6000
k_2	Plant 2 carrying capacity	N_2 mass	1960- 14100	g/ha	<i>Dalea</i> biomass in unburned fields	Tallgrass prairie, Kansas	Towne and Knapp 1996	6000
$\theta_{1,2}$	Per unit mass effect of plant 2 on plant 1 relative to the effect of plant 1 on itself	N_2 mass/ N_1 mass	1.7	g/g	<i>Dalea</i> competition coefficient on <i>Amorpha</i> (1.39, 2.19; upper and lower 95% confidence intervals)	Greenhouse	Pers. obs.	0.56
$\theta_{2,1}$	Per unit mass effect of plant 1 on plant 2 relative to the effect of plant 2 on itself	N_1 mass/ N_2 mass	0.56	g/g	<i>Amorpha</i> competition coefficient on <i>Dalea</i> (0.42, 0.69; upper and lower 95% confidence intervals)	Greenhouse	Pers. obs.	0.56
a_1	Per unit mass herbivore attack rate on plant 1	1/(H mass * time)	0.033	1/g/day				0.033
					Bank vole (<i>Clethrionomys glareolus</i>) attack rates on willow shoots	Controlled environment	Lundberg 1988	
					<i>Microtus ochrogaster</i> and <i>pennsylvanicus</i>	Tallgrass prairie, Iowa	Pers. obs.	

Model			Est.*					Model
param.	Description	Units	(min-max)	Est. units	Study	Location	Source	value used
a_2	Per unit mass herbivore attack rate on plant 2	1/(H mass * time)	0.033	1/g/day	Bank vole (<i>Clethrionomys glareolus</i>) attack rates on willow shoots			0.033
			0.05	1/ind/hour	Bank vole (<i>Clethrionomys glareolus</i>) attack rates on willow shoots	Controlled environment	Lundberg 1988	
			35.972	g/ind	<i>Microtus ochrogaster</i> and <i>pennsylvanicus</i> mean mass	Tallgrass prairie, Iowa	Pers. obs.	
b	Herbivore handling time	(H mass)(time)/(N mass)	1.16	g*days/g	<i>Microtus pennsylvanicus</i> digestion rates	Old field, Michigan	Golley 1960	1.16
m	Per unit mass herbivore mass rate of loss from mortality and respiration	H mass/(H mass)(time)	0.54	g/g/day	<i>Microtus pennsylvanicus</i> daily mass loss from respiration			0.54
			0.518	g/g/day			Berteaux et al. 1996	
			90.31	kJ/day/g	<i>Microtus pennsylvanicus</i> respiration rate	Old field enclosures, Québec	reported in Speakman 1999	
			35.972	g/ind	<i>Microtus ochrogaster</i> and <i>pennsylvanicus</i> mean mass	Tallgrass prairie, Iowa	Pers. obs.	

Model			Est.*					Model
param.	Description	Units	(min- max)	Est. units	Study	Location	Source	value used
						Field sites in		
			5.22	kJ/g	<i>Microtus pennsylvanicus</i> live energy content	Ellis County, Kansas	Fleharty et al. 1973	
			0.023	g/g/day	<i>Microtus pennsylvanicus</i> daily loss from mortality	Field sites in Ellis County, Kansas	Fleharty et al. 1973	
			0.12	kJ/g/day	<i>Microtus pennsylvanicus</i> energy loss from mortality	Old field, Michigan	Golley 1960	
			5.22	kJ/g	<i>Microtus pennsylvanicus</i> live energy content	Field sites in Ellis County, Kansas	Fleharty et al. 1973	
c	Herbivore conversion efficiency	(H mass)/(P mass)	0.70-0.78	g/g				0.7
			0.7	kJ/kJ	<i>Microtus pennsylvanicus</i> assimilation efficiency ((Production+Respiration)/Consumption)	Old field, Michigan	Golley 1960	
			0.78	kJ/kJ	<i>Microtus arvalis</i> assimilation efficiency ((Production+Respiration)/Consumption)	Flood-plain forest, Czechoslovakia	Zejda 1985	
			5.22	kJ/g	Old field, standing green crop energy content	Old field, Michigan	Golley 1960	

Model param.	Description	Units	Est.* (min- max)	Est. units	Study	Location	Source	Model value used
						Field sites in		
					<i>Microtus pennsylvanicus</i> live energy	Ellis County,	Fleharty et al.	
			5.22	kJ/g	content	Kansas	1973	

*All mass values are calculated as fresh (*i.e.*, wet) mass. Plant mass was determined by assuming fresh plant material contains 69.4% water based on water content of prairie forbs (pers. obs.).

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