

Lorente, M., Parsons, W. F. J., Périé, C. and Munson, A. D. 2012. Spectral analysis discerns pattern and feedback in natural- and anthropogenic-disturbed boreal black spruce forests. – *Oikos* 121: 772–782.

## Appendix 1

Cross-spectral analysis is an extension of spectral analysis to two data series (Jenkins and Watts 1968). The cross-spectrum estimator was defined in a manner similar to that of the smoothed spectrum, using the cross-periodogram (Brillinger 1981). Consequently, the cross-spectrum is a complex function obtained by computing a pair of smoothed spectra ( $S_x$  and  $S_y$ ) and a cross-correlation function. The latter complex function can be represented by:

$$S_{xy}^2(f_k) = C_{xy}(f_k) - iQ_{xy}(f_k)$$

where  $C_{xy}(f_k)$  is the co-spectrum and  $Q_{xy}(f_k)$  is the quadrature (quad-) spectrum, which are the respective in-phase and out-of-phase covariances of spatial series  $x$  and  $y$  (Legendre and Legendre 1998). Squared-coherence is a dimensionless measure of the correlation between two data series at a given wave number (Legendre and Legendre 1998, Shumway and Stoffer 2006):

$$\gamma_{xy}(f_k) = \frac{C_{xy}(f_k) + iQ_{xy}(f_k)}{S_x^2(f_k)S_y^2(f_k)}$$

Statistical significance for the coherency spectra was indicated for peaks corresponding to distances over which cycles common to both data series repeated in tandem; the critical value for coherency (0.68 at  $p = 0.0125$ ) was calculated from equations given by Shumway and Stoffer

(2006). The aforementioned co-spectrum further indicates if relationships between two data series are positive or negative (Kachanoski et al. 1985).

## References

Brillinger, D. R. 1981. Time series, data analysis and theory. Expanded edition. – Holden-Day Inc.

Jenkins, G. M. and Watts, D. G. 1968. Spectral analysis and its application. – Holsen Day.

Kachanoski, R. G. et al. 1985. Spatial and spectral relationships of soil properties and microtopography: I. Density and thickness of A horizon. – Soil Sci. Soc. Am. J. 49: 804–812.

Legendre, P. and Legendre, L. 1998. Numerical ecology, 2nd ed. – Elsevier.

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## Appendix 2

Spectral variances (solid line) of data series, i.e. significant (Fig. 1) soil and vegetation properties (defined in Table 1) obtained along one transect (1-m intervals,  $n = 51$  for each transect) on four disturbance types in central Quebec: (A) old harvest (1942), (B) old burn (1906), (C) recent harvest (1988), and (D) recent burn (1986). Dotted horizontal line delimits statistical significance with Bonferroni correction. Shading represents significant peaks, with distances (in m) indicated above each curve. Peaks correspond to distances over which cycles repeat. Distances are the inverse of wave numbers (abscissas).





